We would like to thank I-Hong Hou and Han Deng for catching an error in the proof of Theorem 4.

Theorem 4 is corrected. The conclusion of Theorem 4 should be "In a general multihop network topology with general arrival samples, all online algorithms are  $\Omega(\log P_M)$ -competitive", rather than "In a general multihop network topology with general arrival samples, all online algorithms are  $\Omega(P_M \log P_M)$ -competitive".

The derivation of  $\sum_{j=1}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} F_j$  bound in page 9 is corrected as follows:

$$\begin{split} & s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M) \\ & \sum_{j=1}^{j=1} F_j \\ &= \sum_{j=1}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} \frac{1}{\rho_j} \frac{P_M}{\lceil \frac{\rho_m}{\rho_M s_M} 2^{\lfloor \frac{j}{s_M^2 P_M} \rfloor} \rceil} \sum_{i=1}^j x_i \\ &= \sum_{i=1}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} \\ &= \sum_{j=i}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} \frac{1}{\rho_j} \frac{P_M}{\lceil \frac{\rho_m}{\rho_M s_M} 2^{\lfloor \frac{j}{s_M^2 P_M} \rfloor} \rceil} \right) x_i \\ &\leq \sum_{i=1}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} \frac{1}{\rho_i} \frac{P_M}{\lceil \frac{\rho_m}{\rho_M s_M} 2^{\lfloor \frac{j}{s_M^2 P_M} \rfloor} \rceil} \\ &\left(1 + s_M^2 P_M \frac{\rho_M}{\rho_m} \sum_{j=0}^{\log(\frac{\rho_M}{\rho_m} s_M P_M)} \frac{1}{2^j}\right) x_i \\ &\leq \sum_{i=1}^{s_M^2 P_M \log(\frac{\rho_M}{\rho_m} s_M P_M)} 2 s_M^2 P_M \frac{\rho_M}{\rho_m} x_i \frac{1}{\rho_i} \frac{P_M}{\lceil \frac{\rho_m}{\rho_M s_M} 2^{\lfloor \frac{j}{s_M^2 P_M} \rfloor} \rceil} \\ &\leq 2 \frac{\rho_M}{\rho_m} s_M^3 P_M^3, \end{split}$$

And the subsequent part of Theorem 4's proof is modified accordingly and leads to the conclusion that the optimal online algorithm is  $O(\log P_M)$ -competitive.

With the above change, some sentences that claim the proposed algorithm in Section V is order-optimal online algorithm no longer hold as the byproduct of Theorem 4. Our proposed algorithm is now sub-optimal as it is  $O(P_M \log P_M)$ -competitive. We have changed these sentences in the paper as well.

The whole paper with the corrections can be found in <u>https://ia601508.us.archive.org/27/items/HardDeadlineSchedErrata/OptimalOnlin</u> eSchedulingWithArbitraryHardDeadlinesInMultihopCommunicationNetworks.pdf